JEE-MAIN EXAM APRIL, 2025

Date: - 08-04-2025 (SHIFT-2)

MATHEMATICS

SECTION-A

If A and B are two events such that P(A) = 0.7, P(B) = 0.4 and $P(A \cap \overline{B}) = 0.5$, where \overline{B} denotes 1. the complement of B, then $P(B|(A \cup \overline{B}))$ is equal to (1) $\frac{1}{2}$ (2) $\frac{1}{4}$ (3) $\frac{1}{6}$ (4) $\frac{1}{2}$ Let the function $f(x) = \frac{x}{3} + \frac{3}{x} + 3, x \neq 0$ be strictly increasing in $(-\infty, \alpha_1) \cup (\alpha_2, \infty)$ and strictly 2. decreasing in $(\alpha_3, \alpha_4) \cup (\alpha_4, \alpha_5)$. Then $\sum_{i=1}^5 \alpha_i^2$ is equal to (1) 48 (4) 40 (3) 28 Let $A = \begin{bmatrix} 2 & 2+p & 2+p+q \\ 4 & 6+2p & 8+3p+2q \\ 6 & 12+3p & 20+6p+3q \end{bmatrix}$. If det(adj (adj (3A))) = $2^m \cdot 3^n, m, n \in \square$, then m+n is 3. equal to (2) 20(3) 26 (4) 24 (1) 22 Let the ellipse $3x^2 + py^2 = 4$ pass through the centre *C* of the circle $x^2 + y^2 - 2x - 4y - 11 = 0$ of 4. radius r. Let f_1, f_2 be the focal distances of the point C on the ellipse. Then $6f_1f_2 - r$ is equal to (1) 68 (2) 78 (3) 70 (4) 74 Let *a* be the length of a side of a square OABC with O being the origin. Its side OA makes an acute 5. angle α with the positive x-axis and the equations of its diagonals are $(\sqrt{3}+1)x + (\sqrt{3}-1)y = 0$ and $(\sqrt{3}-1)x - (\sqrt{3}+1)y + 8\sqrt{3} = 0$. Then a^2 is equal to

6. If
$$\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \dots = \frac{\pi^4}{90}$$

 $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots = \alpha, \frac{1}{2^4} + \frac{1}{4^4} + \frac{1}{6^4} + \dots = \beta$ then $\frac{\alpha}{\beta}$ is equal to
(1) 15 (2) 23 (3) 18 (4) 14



7.	Let $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$ and $\vec{b} = 2\hat{i} + \hat{j} - \hat{k}$. Let \hat{c} be a unit vector in the plane of the vectors \vec{a} and \vec{b}								
	and be perpendicular to $ec{a}$. Then such a vector \hat{c} is :								
	(1) $\frac{1}{\sqrt{5}}(\hat{j}-2\hat{k})$ (2) $\frac{1}{\sqrt{3}}(\hat{i}-\hat{j}+\hat{k})$ (3) $\frac{1}{\sqrt{3}}(-\hat{i}+\hat{j}-\hat{k})$ (4) $\frac{1}{\sqrt{2}}(-\hat{i}+\hat{k})$								
8.	Let $f(x) = x - 1$ and $g(x) = e^x$ for $x \in \Box$. If $\frac{dy}{dx} = \left(e^{-2\sqrt{x}}g(f(f(x))) - \frac{y}{\sqrt{x}}\right), y(0) = 0$, then $y(1)$ is								
	(1) $\frac{2e-1}{e^3}$ (2) $\frac{e-1}{e^4}$ (3) $\frac{1-e^3}{e^4}$ (4) $\frac{1-e^2}{e^4}$								
9.	Let the values of λ for which the shortest distance between the lines $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$ and								
	$\frac{x-\lambda}{3} = \frac{y-4}{4} = \frac{z-5}{5}$ is $\frac{1}{\sqrt{6}}$ be λ_1 and λ_2 . Then the radius of the circle passing through the points								
	$(0,0), \left(\lambda_1,\lambda_2 ight)$ and $\left(\lambda_2,\lambda_1 ight)$ is								
	(1) 3 (2) 4 (3) $\frac{5\sqrt{2}}{3}$ (4) $\frac{\sqrt{2}}{3}$								
10.	A line passing through the point $P(a,0)$ makes an acute angle α with the positive x-axis. Let this								
	line be rotated about the point P through an angle $\frac{\alpha}{2}$ in the clock-wise direction. If in the new position,								
	the slope of the line is $2-\sqrt{3}$ and its distance from the origin is $\frac{1}{\sqrt{2}}$, then the value of								
	$3a^2 \tan^2 \alpha - 2\sqrt{3}$ is								
	(1) 8 (2) 6 (3) 5 (4) 4								
11.	Let $A = \left\{ \theta \in [0, 2\pi] : 1 + 10 \operatorname{Re}\left(\frac{2\cos\theta + i\sin\theta}{\cos\theta - 3i\sin\theta}\right) = 0 \right\}$. Then $\sum_{\theta \in A} \theta^2$ is equal to								
	(1) $\frac{27}{4}\pi^2$ (2) $6\pi^2$ (3) $8\pi^2$ (4) $\frac{21}{4}\pi^2$								
12.	Given below are two statements:								
	Statement I: $\lim_{x \to 0} \left(\frac{\tan^{-1} x + \log_e \sqrt{\frac{1+x}{1-x}} - 2x}{x^5} \right) = \frac{2}{5}$								

Statement II : $\lim_{x \to 1} \left(x^{\frac{2}{1-x}} \right) = \frac{1}{e^2}$

In the light of the above statements, choose the correct answer from the options given below

- (1) Both Statement I and Statement II are true (2) Statement I is false but Statement II is true
- (3) Both Statement I and Statement II are false (4) Statement I is true but Statement II is false



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13. The integral
$$\int_{-1}^{\frac{1}{2}} \left(\left| \pi^{2} x \sin(\pi x) \right| dx \text{ is equal to} \right)$$
(1) $2 + 3\pi$
(2) $4 + \pi$
(3) $1 + 3\pi$
(4) $3 + 2\pi$
(5) $1 + 3\pi$
(7) $2 + 3\pi$
(7) $2 + \pi$
(8) $1 + 3\pi$
(9) $3 + 2\pi$
(9) $3 + 2\pi$
(9) $3 + 2\pi$
(1) There are 12 points in a plane, no three of which are in the same straight line, except 5 points which are collinear. Then the total number of triangles that can be formed with the vertices at any three of these 12 points is
(1) 230
(2) 200
(3) 210
(4) 220
(5) Let $A = [0, 1, 2, 3, 4, 5]$. Let R be a relation on A defined by $(x, y) \in R$ if and only if max $\{x, y\} \in [3, 4]$. Then among the statements
(5, 1) The number of elements in R is 18, and
(5, 1) The relation R is symmetric but neither reflexive nor transitive
(1) only (5, 1) is true
(2) both are false
(3) only (5, 2) is true
(4) both are true
(5) The squares of the roots of $|x-2|^{2} + |x-2| - 2 = 0$ and the squares of the roots of $x^{2} - 2|x-3| - 5 = 0$, is
(1) 26
(2) 30
(3) 24
(4) 36
(1) $\pi + \frac{5}{2}$
(2) $\pi - \frac{3}{2}$
(3) $\pi - \frac{5}{4}$
(4) $\pi + \frac{3}{2}$
(3) $\pi + \frac{5}{2}$
(4) $\pi + \frac{3}{2}$
(4) Let $f(x)$ be a positive function and $I_{1} = \int_{-\frac{1}{2}}^{1} 2f(2x(1-2x))dx$ and $I_{2} = \int_{-1}^{2} f(x(1-x))dx$. Then the value of $\frac{I_{2}}{I_{1}}$ is equal to
(1) $\pi + \frac{5}{2}$
(2) $\pi - \frac{3}{2}$
(3) 4
(4) 12
(1) $\pi + \frac{3}{2}$
(1) $4\pi + \frac{16}{1} = \frac{16}{1} = \frac{13}{2} = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}$. If $\frac{1}{\alpha^{4}} + \frac{\pi}{\alpha^{5}} + \frac{\pi}{\alpha^{5}} = 3$, then $m + n$ is equal to
(1) 11
(2) 3
(3) 7
(4) 8
(1) 11
(2) 3
(3) 7
(4) 8
(2) Extended at the sequence of $x^{2} + x + 1 = 0$, and for some a and b in
(1) 11
(2) 3
(3) 7
(4) 8
(2) Extended at the sequence of $x^{2} + x + 1 = 0$, and for some a and b in
(1) 11
(2) 3
(3) 7
(4) 8
(3) 7
(4) 8
(3) 7
(4) 8

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20. The number of integral terms in the expansion of $\left(5^{\frac{1}{2}} + 7^{\frac{1}{8}}\right)^{1016}$ is

(1) 129 (2) 128 (3) 130 (4) 127

SECTION-B

21. The product of the last two digits of (1919)¹⁹¹⁹ is _____

- **22.** Let the area of the bounded region $\{(x, y): 0 \le 9x \le y^2, y \ge 3x 6\}$ be A. Then 6A is equal to
- **23.** Let *r* be the radius of the circle, which touches *x* axis at point (a,0), a < 0 and the parabola $y^2 = 9x$ at the point (4,6). Then *r* is equal to _____.
- 24. Let the domain of the function $f(x) = \cos^{-1}\left(\frac{4x+5}{3x-7}\right)$ be $[\alpha,\beta]$ and the domain of

 $g(x) = \log_2(2 - 6\log_{27}(2x+5))$ be (γ, δ) .

Then $|7(\alpha + \beta) + 4(\gamma + \delta)|$ is equal to_____

25. Let the area of the triangle formed by the lines x+2=y-1=z, $\frac{x-3}{5}=\frac{y}{-1}=\frac{z-1}{1}$ and

 $\frac{x}{-3} = \frac{y-3}{3} = \frac{z-2}{1}$ be *A*. Then A² is equal to_____.

NTA ANSWERS													
1.	(2)	2.	(2)	3.	(4)	4.	(3)	5.	(5)	6.	(1)	7.	(4)
8.	(2)	9.	(3)	10.	(4)	11.	(4)	12.	(1)	13.	(3)	14.	(3)
15.	(3)	16.	(4)	17.	(3)	18.	(3)	19.	(1)	20.	(2)	21.	(63)
22.	(15)	23.	(30)	24.	(96)	25.	(56)						

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